

Fig. 1. $\left[\mathrm{Ca}\left(\mathrm{H}_{2} \mathrm{O}\right)_{7}\right]\left[\mathrm{Cd}_{2} \mathrm{Br}_{6}\right]$ viewed down the $a$ axis.
Discussion. Crystals of the title compound were formed when a flask containing a saturated solution of $\mathrm{CaBr} 2: \mathrm{CdBr}_{2}$ in equilibrium with the solid was opened to the air. The original crystals which dissolved at the same time have the composition $\mathrm{CaCd}_{2} \mathrm{Br}_{6} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (Balarew, Duhlev \& Panaiotov, 1982). The bonding of

Ca to water and Cd to Br in $\left[\mathrm{Ca}\left(\mathrm{H}_{2} \mathrm{O}\right)_{7}\right]\left[\mathrm{Cd}_{2} \mathrm{Br}_{6}\right]$ confirms the predictions of Balarew \& Duhlev (1984) whose work prompted the present study. The interatomic distances are close to those expected. The $\mathrm{Ca}\left(\mathrm{H}_{2} \mathrm{O}\right)_{7}^{2+}$ and infinite chain $\mathrm{Cd}_{2} \mathrm{Br}_{6}^{2-}$ ions are linked by hydrogen bonds with $\mathrm{O} \cdots \mathrm{Br}$ distances ranging from 3.30 to over $3.60 \AA$.

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# Structure of Lead(II) Copper(I) Arsenate(V) 

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#### Abstract

PbCuAsO}_{4}, M_{r}=409.65\), triclinic, $P \overline{1}, a$ $=4.832$ (1), $\quad b=5.837$ (1), $\quad c=7.995$ (2) $\AA, \quad \alpha=$ 78.68 (2), $\quad \beta=74.95$ (1), $\quad \gamma=84.04$ (1) ${ }^{\circ}, \quad V=$ $213.2 \AA^{3}, Z=2, \quad D_{x}=6.382 \mathrm{Mg} \mathrm{m}^{-3}$, Мо $K \alpha, \lambda=$ $0.710688 \AA, \mu=50.3 \mathrm{~mm}^{-1}, F(000)=352$, room temperature, $R=0.030$ for 1039 observed reflections up to $\sin \theta / \lambda=0.70 \AA^{-1} . \mathrm{PbCuAsO}_{4}$ crystallizes in a network structure built up by three characteristic cation coordination polyhedra. The Pb atom is irregularly $[4+2]$ coordinated by six O atoms. The monovalent Cu atom has a linear [2] coordination, and the pentavalent As atom has the usual tetrahedral [4] coordination by O atoms. $\mathrm{PbCuAsO}{ }_{4}$ was synthesized under hydrothermal conditions [490 (5) K, saturation vapour pressure].


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Introduction. The oxidation state of arsenic in oxygen compounds indicates in mineralogy the conditions of formation of various ore deposits and their weathering during geologic periods. Therefore investigations within the system $\mathrm{PbO}, \mathrm{CuO}, \mathrm{As}_{2} \mathrm{O}_{3}$ and $\mathrm{H}_{2} \mathrm{O}$ under hydrothermal conditions were performed to learn the different conditions for the formation of arsenite and arsenate minerals (Pertlik, 1977).

Experimental. $\mathrm{PbCuAsO}_{4}$ is a product of the following chemical reaction: 2 g of an equimolar mixture of PbO , CuO , and $\mathrm{As}_{2} \mathrm{O}_{3}$ were placed in a 'Teflon'-coated vessel ( $V \simeq 6000 \mathrm{~mm}^{3}$ ) and the vessel was filled to $\sim 80 \%$ of its volume with $1 M$ acetic acid. After heating for 4 d , © 1986 International Union of Crystallography
temperature 490 (5) K, crystals of the following compounds were found in the reaction mixture: $\mathrm{Cu}_{2} \mathrm{O}$ (cuprite), $\mathrm{CuAs}_{2} \mathrm{O}_{4}$ (trippkeite), and $\mathrm{PbCuAsO}_{4}$ (weight ratio $\simeq 1: 1: 5$ ). Crystal sizes of all three compounds are approximately $0.10 \mathrm{~mm}^{3}$. Grains of $\mathrm{PbCuAsO}_{4}$ are colourless, transparent, with high lustre. The atomic ratio of the elements $\mathrm{Pb}, \mathrm{As}$, and Cu was determined by electron-microprobe analysis, the oxidation state of the elements and the chemical formula by the crystal structure analysis. It is worth mentioning that for the formation of $\mathrm{PbCuAsO}_{4}$ crystals the following reactions took place: $\mathrm{Cu}^{\mathrm{II}}$ was reduced to $\mathrm{Cu}^{1}$ in combination with an oxidation of $\mathrm{As}^{\mathrm{III}}$ to $\mathrm{As}^{\mathrm{V}}$. Under the given conditions, $T \leq 500 \mathrm{~K}$, saturation vapour pressure, the formation of $\mathrm{PbCuAsO}_{4}$ from a mixture of $\mathrm{Cu}_{2} \mathrm{O}, \mathrm{PbO}$ and an $\mathrm{As}^{\mathrm{v}}$ oxide solution was not successful with acetic acid or water as solvent.

X-ray work: Stoe AED 2 four-circle diffractometer, graphite-monochromatized Mo $K \alpha$ radiation, $2 \theta / \omega$ scan, min. step number 35 increased for ( $\alpha_{1}, \alpha_{2}$ ) splitting, step width $0.03^{\circ}$, step time 0.5 to 1.5 s per step, data collection up to $2 \theta=60^{\circ}$; three standard reflections, no significant intensity variation. Crystal size: $0.114 \times 0.095 \times 0.019 \mathrm{~mm}$. Lattice parameters from 30 reflections up to $2 \theta=50^{\circ}$. Numerical absorption correction according to crystal shape (transmission factors from 0.250 to 0.412 ). 1326 measured reflections ( $h:-7 \rightarrow 7, k:-8 \rightarrow 8, l:-1 \rightarrow 11$ ) were merged; 1142 unique data of which 103 are less than $3 \sigma\left(F_{o}\right)$. $R=0.030$ and $w R=0.026, w=1 /\left[\sigma\left(F_{o}\right)\right]^{2} ;$ max. $\Delta / \sigma<10^{-3}$; max. and min. heights in final difference Fourier map 1.79 and $-1.86 \mathrm{e} \AA^{-3} . g$ for isotropic secondary extinction (Zachariasen, 1967) is 4.88 (16) $\times 10^{-5}$.

Correction for Lorentz and polarization effects; complex scattering functions for neutral atoms (International Tables for X-ray Crystallography, 1974). All calculations were performed with the program system STRUCSY (Fa. Stoe \& Cie, Darmstadt). Structure solved by direct methods, which yielded the positions of the metal atoms. Subsequent Fourier synthesis showed the atomic coordinates of the O atoms. Several cycles of full-matrix least-squares refinements on $F$ with anisotropic temperature parameters. Structure parameters are listed in Table 1.* Some important interatomic distances are summarized in Table 2.

Discussion. The Pb atom is irregularly [4+2] coordinated by six O atoms. Such an irregular coordination polyhedron is typical for the crystal-chemical behaviour

[^0]not only of divalent lead but also of all elements with a 'stereometric activity' of the lone-pair electrons (cf. for lead: Sahl, 1970). The next cation neighbour of the Pb atom is a Cu atom. The distance $\mathrm{Pb}-\mathrm{Cu}=3.325$ (1) $\AA$ is in the same range as the sum of the metallic radii of these two elements and it seems therefore that it should not be considered a chemical bond. Worth mentioning is that two of the $\mathrm{O}-\mathrm{O}$ edges within the Pb coordination figure are very short $[O(2)-O(2)=2.74$ (1) and $\mathrm{O}(4)-\mathrm{O}(4)=2.77(1) \AA$, but both these atom pairs represent further common edges between two Pb coordination figures.

Table 1. Fractional atomic coordinates with e.s.d.'s in parentheses and equivalent isotropic temperature parameters (space group $P \overline{1}$, all atoms at general positions)

| $U_{\text {eq }}=\left(B_{11}+B_{22}+B_{33}\right) / 3$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $x$ | $y$ | $z$ | $U_{\text {eq }}\left(\dot{\AA}^{2}\right)$ |
| Pb | 0.9387 (1) | 0.7103 (1) | 0.6760 (1) | 0.014 |
| Cu | 0.6346 (3) | $0 \cdot 1969$ (2) | 0.0043 (2) | 0.021 |
| As | 0.4218 (2) | $0 \cdot 2030$ (1) | 0.6866 (1) | 0.011 |
| O(1) | 0.7672 (14) | 0.0289 (12) | 0.1919 (11) | 0.019 |
| O(2) | 0.7313 (12) | 0.0953 (11) | 0.5642 (11) | 0.015 |
| O(3) | 0.5091 (14) | 0.6306 (11) | 0.1787 (11) | 0.021 |
| O(4) | 0.7762 (12) | 0.6262 (10) | 0.4391 (10) | 0.013 |

Table 2. Some selected bond lengths ( $\AA$ ) with e.s.d.'s in parentheses for $\mathrm{PbCuAsO}_{4}$

| $\mathrm{Pb}-\mathrm{O}(2)$ | $2.334(7)$ | $\mathrm{Cu}-\mathrm{O}(1)$ | $1.848(8)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{Pb}-\mathrm{O}(4)$ | $2.380(7)$ | $\mathrm{Cu}-\mathrm{O}(3)$ | $1.855(8)$ |
| $\mathrm{Pb}-\mathrm{O}\left(2^{\prime}\right)$ | $2.462(6)$ | $\mathrm{As}-\mathrm{O}(1)$ | $1.699(7)$ |
| $\mathrm{Pb}-\mathrm{O}\left(4^{\prime}\right)$ | $2.468(6)$ | $\mathrm{As}-\mathrm{O}(2)$ | $1.696(7)$ |
| $\mathrm{Pb}-\mathrm{O}(1)$ | $2.704(7)$ | $\mathrm{As}-\mathrm{O}(3)$ | $1.697(7)$ |
| $\mathrm{Pb}-\mathrm{O}(3)$ | $2.945(7)$ | $\mathrm{As}-\mathrm{O}(4)$ | $1.681(6)$ |



Fig. 1. Projection of the crystal structure of $\mathrm{PbCuAsO}_{4}$ on to (100). The short $\mathrm{O}-\mathrm{O}$ edges between the $\mathrm{PbO}_{6}$ coordination polyhedra are dotted lines $(\mathrm{O}-\mathrm{O}<2.8 \AA)$. The $\mathrm{Pb}-\mathrm{O}$ distances from 2.50 to $3.00 \AA$ are drawn as broken lines. The atoms are labelled with $x$.

The Cu atom has an almost linear [2] coordination by O atoms $\left[\mathrm{O}(1)-\mathrm{Cu}-\mathrm{O}(3)=178 \cdot 1(5)^{\circ}\right]$. Such a coordination is usual for monovalent Cu (cf. Wells, 1984). A comparable example is the structure of $\mathrm{Cu}_{2} \mathrm{O}$ with a symmetry-restricted linear [2] coordination and $\mathrm{Cu}-\mathrm{O}$ distances of $1.84 \AA$ (Eichhorn, Spilker \& Fischer, 1984).

The coordination polyhedron of the As atom is a tetrahedron, built up by four crystallographically different O atoms. As shown in Table 2, the four As-O distances are equal within two e.s.d.'s. Also the range of variation of the $\mathrm{O}-\mathrm{O}$ distances [2.71 (1) to 2.80 (1) $\AA$ ] within the $\mathrm{AsO}_{4}$ tetrahedron is small.

The $\mathrm{PbO}_{6}$ coordination polyhedra and the $\mathrm{AsO}_{4}$ tetrahedra are connected in two dimensions, resulting in a formal $\left[\mathrm{PbAsO}_{4}\right]$ sheet parallel to $(001)$. These sheets are combined via strong $\mathrm{Cu}-\mathrm{O}$ bonds involving the monovalent Cu atom to form a network structure.

The main features of the atcmic arrangements are represented in Fig. 1.

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# Structure of Deuterated Triammonium Hydrogendisulfate, $\dagger\left(\mathbf{N D}_{4}\right)_{3} \mathbf{D}\left(\mathbf{S O}_{4}\right)_{2}$. Phases (III') and (VI) 

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#### Abstract

Phase (III'): $M_{r}=260 \cdot 3$, monoclinic, $P 2$, $a=10.087$ (2), $b=5.835$ (1), $c=15.542$ (2) $\AA, \beta=$ $101.71(2)^{\circ}, \quad V=895.7 \AA^{3}, \quad Z=4, \quad D_{x}=$ $1.930 \mathrm{Mg} \mathrm{m}^{-3}$, Mo $K \alpha, \lambda=0.7107 \AA, \mu=0.60 \mathrm{~mm}^{-1}$, $F(000)=521 \cdot 84, T=189 \pm 7 \mathrm{~K}, R=0.028$ for 2156 unique reflections. Phase (VI): triclinic, $P 1, a=$ $10 \cdot 123$ (1), $\quad b=5.846$ (1),$\quad c=15 \cdot 476$ (1) $\AA, \quad a=$ 89.98 (1), $\quad \beta=101.78$ (1), $\quad \gamma=90.01$ (1) ${ }^{\circ}, \quad V=$ $896.6 \AA^{3}, Z=4, \quad D_{x}=1.928 \mathrm{Mg} \mathrm{m}^{-3}$, Мо $K \alpha, \lambda=$ $0.7107 \AA, \mu=0.60 \mathrm{~mm}^{-1}, F(000)=521.84, T=233$ $\pm 7 \mathrm{~K}, R=0.035$ for 4367 unique reflections. The structures in phases (III') and (VI) have pseudo P2/c symmetry. It has been found that the ferroelectric polarization observed in phase (VI) is mainly caused by the arrangement of the distorted $\mathrm{SO}_{4}^{2-}$ ions. The polarization along $\mathbf{c}^{*}$ is expected to be easily reversed by slightly changing the $\mathrm{SO}_{4}^{2-}$ geometries.


Introduction. Triammonium hydrogendisulfate, $\left(\mathrm{NH}_{4}\right)_{3} \mathrm{H}\left(\mathrm{SO}_{4}\right)_{2}$, at 0.1 MPa shows successive phase transitions and has six phases (I), (II), (III), (IV), (V),

[^1](VII) (Gossner, 1904; Fischer, 1914; Gesi, 1976a; Gesi \& Ozawa, 1977; Suzuki, 1979; Suzuki, Oshino, Gesi \& Makita, 1979; Gesi, 1980); phase (VII) shows ferroelectricity (Gesi, 1980). Another ferroelectric phase, (VI), exists at a hydrostatic pressure higher than about 500 MPa (Gesi, 1976b).

The deuterated crystal also exhibits complicated successive phase transitions; the six isostructural phases at 0.1 MPa are designated (I), (II), (III), (VI), (III') and (VII) with descending temperature (Osaka, Makita \& Gesi, 1977; Gesi, Ozawa, Osaka \& Makita, 1980). The ferroelectric phase (VI) appears at 0.1 MPa , showing an isotope effect. Recently, phases (IX) and (VIII) were found at hydrostatic pressures higher than about 300 MPa and about 450 MPa (Osaka, Makita \& Gesi, 1980).

Gesi (1977) suggested that the modified Mitsui (1958) model was effective for explaining the dielectric behaviour of $\left(\mathrm{NH}_{4}\right)_{3} \mathrm{H}\left(\mathrm{SO}_{4}\right)_{2}$. However, the details of the phase transitions and the origin of the spontaneous polarization are not explained well. The $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ hydrogen bonds, which link neighbouring $\mathrm{SO}_{4}^{2-}$ ions, are influenced by deuteration; the $\mathbf{O} \cdots \mathrm{O}$ bond length is


[^0]:    * Lists of structure and thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 42844 ( 14 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

[^1]:    $\dagger \operatorname{Tri}\left({ }^{2} \mathrm{H}_{4}\right)$ ammonium deuteriumbis(sulfate).

